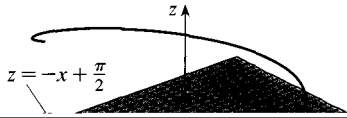


□ Figure 8 shows the helix and the osculating plane in Example 7.



**SOLUTION** The normal plane at  $P$  has normal vector  $\mathbf{r}'(\pi/2) = \langle -1, 0, 1 \rangle$ , so an equation is

$$-1(x - 0) + 0(y - 1) + 1\left(z - \frac{\pi}{2}\right) = 0 \quad \text{or} \quad z = x + \frac{\pi}{2}$$

The osculating plane at  $P$  contains the tangent  $\mathbf{T}$  and  $\mathbf{N}$  as its normal vectors.

10. Reparametrize the curve

$$\mathbf{r}(t) = \left( \frac{2}{3}t^3 - 1 \right) \mathbf{i} + \frac{2t}{3} \mathbf{j}$$

(b) Estimate the curvature at  $P$  and at  $Q$  by sketching the osculating circles at those points.

curve and its curvature function  $\kappa(x)$  on the same screen. Is the